



ECOM+2

– Upcoming model developments

Prof. Per AGRELL

Prof. Peter BOGETOFT

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Outline

Basic measures

- Official and unofficial ECOM+ scores

Comparability

- Economies of scale and scope
- Currency and inflation adjustments

Decomposition

- Cost, OpEx and CapEx efficiency
- Fox Paradox
- Directional efficiency

Dynamics

- Malmquist efficiencies
- Linkage problem and fixed base Malmquist
- Forgiveness factor

Conclusions



Basic measures



ECOM+ Structure

	Benchmarked OPEX		Normalized CAPEX
UnitCost	$C_{ff} + \sum_{s=t_0}^t \varphi_s I_{fs} \alpha(r, T_f)$		
$UC_{ff}(w, v) =$	$\sum_a N_{fa} w_{fa} + \sum_{s=t_0}^t \sum_a \varphi_s n_{fas} v_{fa} \alpha(r, T_g)$		
	Standard OPEX		Standard CAPEX



ECOM+ Measures

Unit costs is cost per grid unit

$$UC = \text{cost} / \text{grid size}$$

Benchmark is company with lowest unit costs

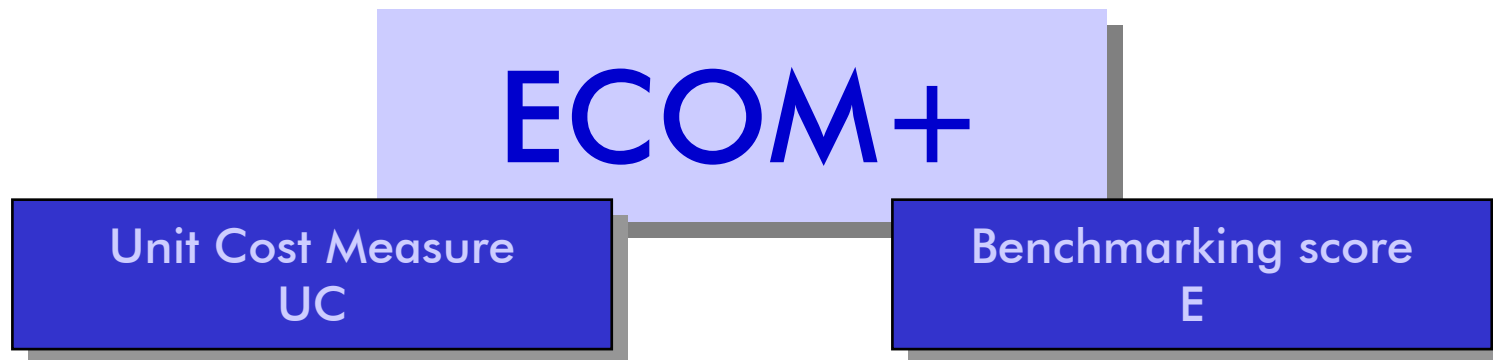
$$\text{Benchmark} = \min \{ \text{unit costs} \}$$

Efficiency is

$$E = \text{benchmark} / \text{unit cost}$$



ECOM+ is a dual method



How well are we
doing in compared to a norm?

How well are we
doing relative to the others?



Unofficial ECOM+ measures

Background

- The ECOM+ reported additional information
- TSOs and regulators studied and used
 - OpEx efficiency
 - CapEx efficiency

Motivations

- Controllability
- Regulation
- Learning
- Comparability
-



Partial OpEx and CapEx scores

$$\begin{array}{c}
 \text{UnitCost} \\
 UC_{ff}(w, v) =
 \end{array}
 \begin{array}{c}
 \text{OPEX} \\
 C_{ff}
 \end{array}
 +
 \begin{array}{c}
 \text{CAPEX} \\
 \sum_{s=t_0}^t \varphi_s I_{fs} \alpha(r, T_f)
 \end{array}
 \begin{array}{c}
 \text{OPEX Grid Size} \\
 \sum_a N_{fa} w_{fa}
 \end{array}
 +
 \begin{array}{c}
 \text{CAPEX Grid Size} \\
 \sum_{s=t_0}^t \sum_a \varphi_s n_{fas} v_{fa} \alpha(r, T_g)
 \end{array}$$

OpEx UnitCost
CapEx UnitCost



Comparability



Economies of scale

ECOM+ evaluates and compares

- $\text{UnitCosts} = \text{Costs}/\text{GridSize}$

Implicit assumption is

- CRS = constant return to scale

Could be relaxed

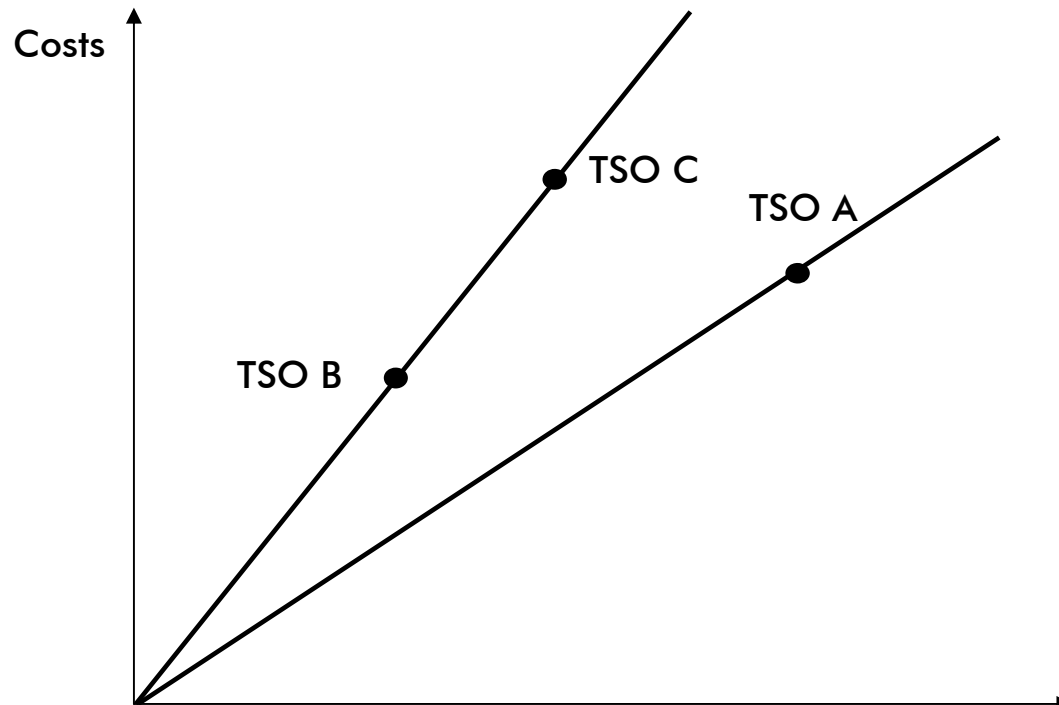
- VRS, NDRS, RCRS, FDH,... ...

Not main priority

- ECOM+ results did not contradict crs: both small and large TSO were efficient
- Too few data points to make a full test
- Appropriate size measure could depend on asset distribution: small TSO with few assets types could have same economies of scale as large TSO with numerous asset types.



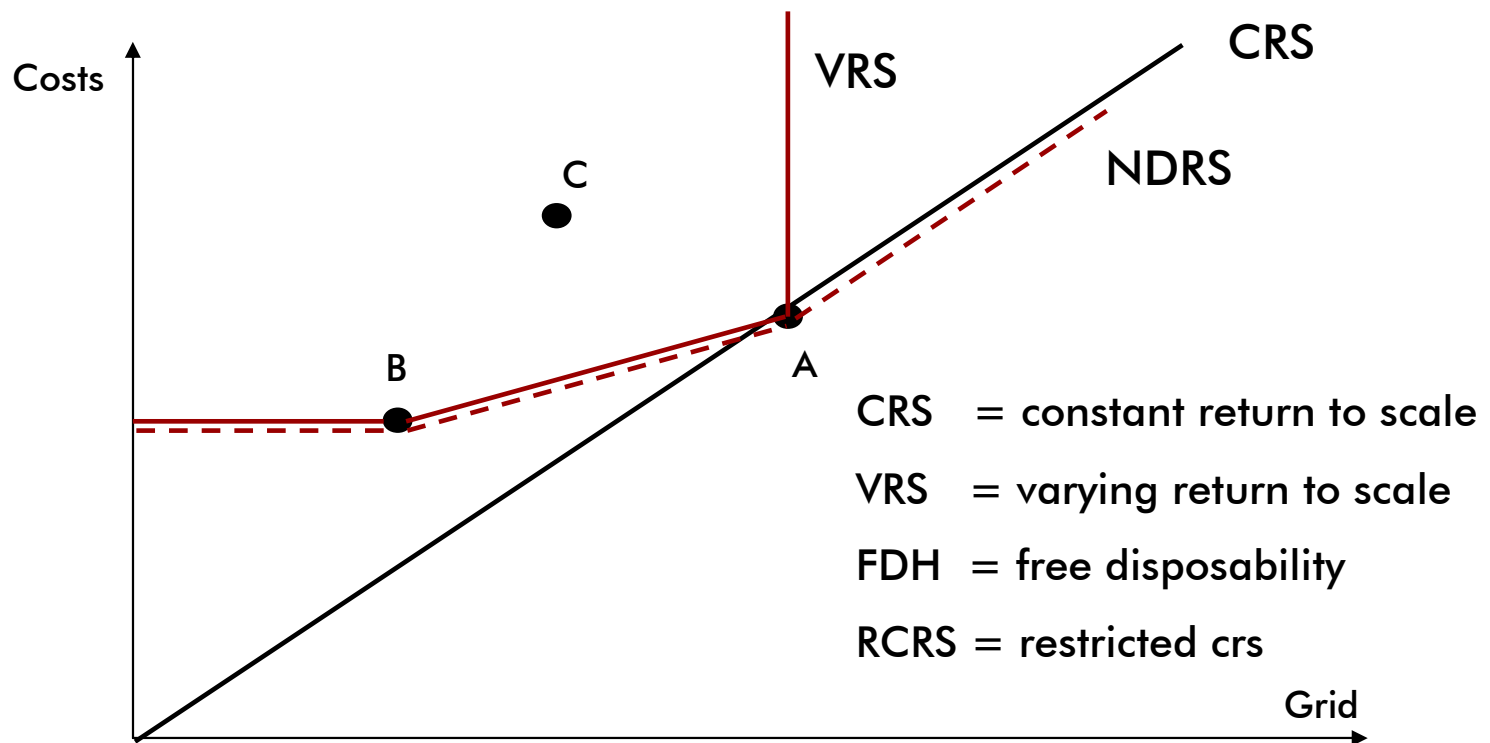
Constant return to scale



Unit Cost = Slope of line
TSO B and C same Unit Costs.
TSO A lower Unit Costs



Alternative scale models





Economies of scope

ECOM+ evaluates and compares

- OpEx+CapEx

Implicit assumption is

- Perfect cost substitution OR
- Allocative efficiency

Could be relaxed

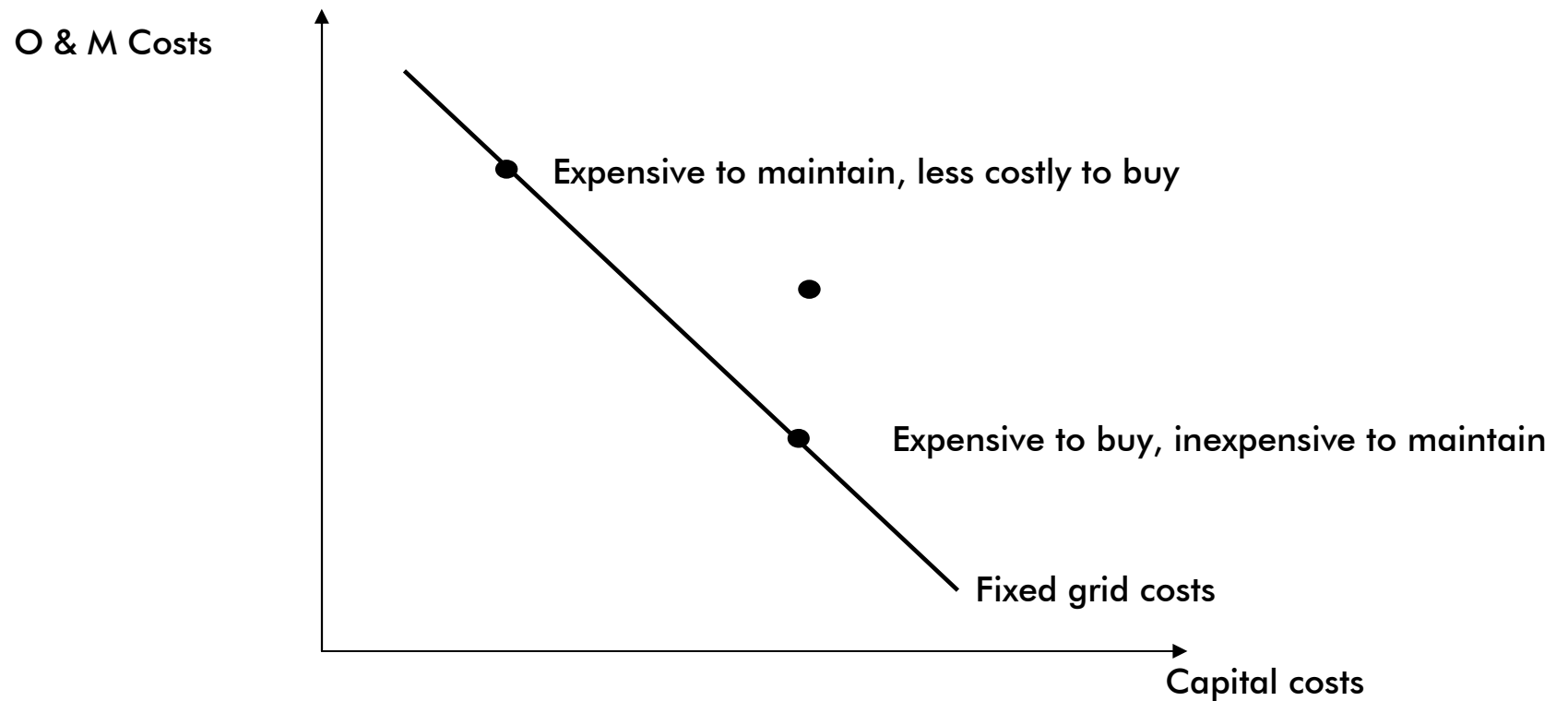
- Limited OpEx and CapEx substitution
- FDH, Convexity, Linearity

Important ?

- NO
 - If TSO is responsible for allocative decisions
- YES
 - Controllability
 - Regulatory uses
 - Present or past merits



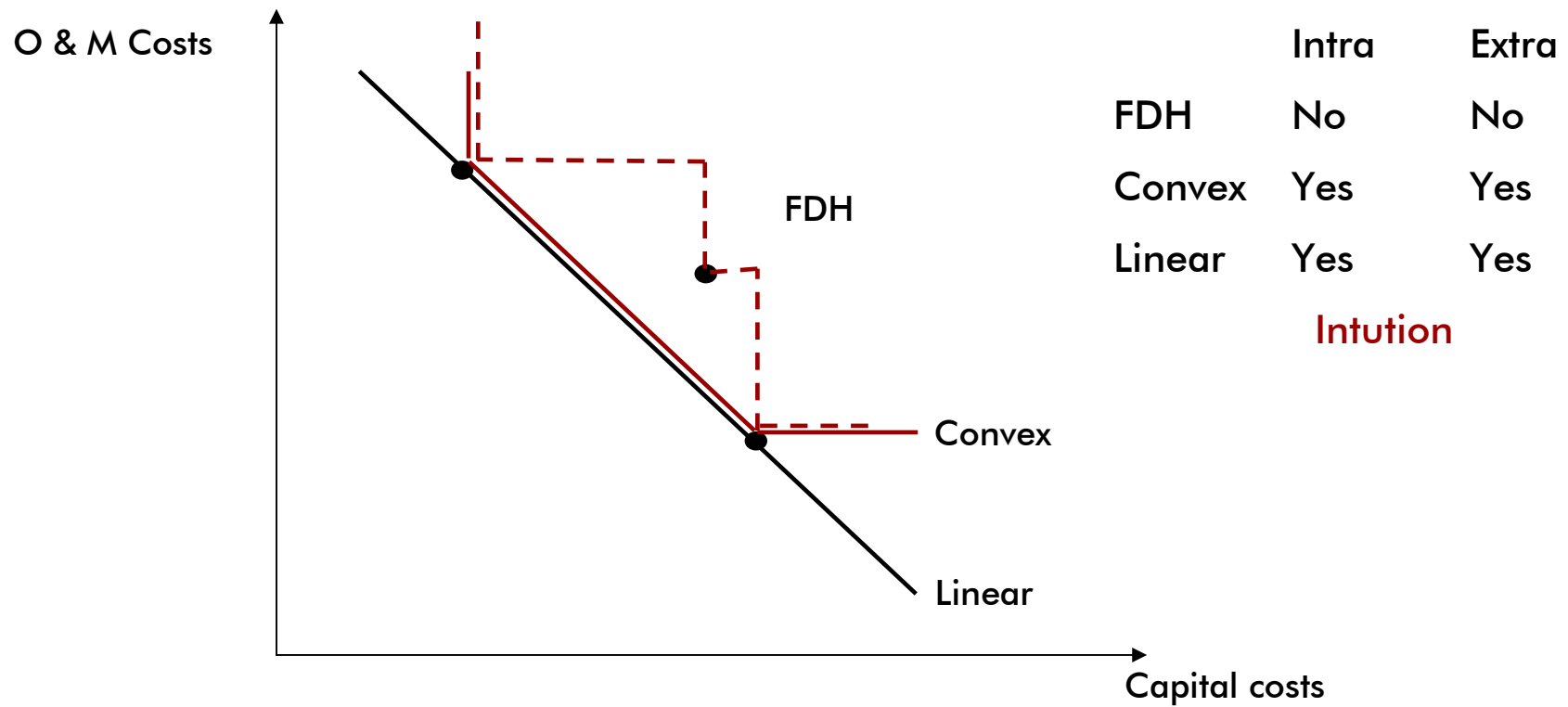
Perfect cost substitution



O & M and capital costs added to capture substitution



Alternative scope models





Decomposition



Three unit costs

	OPEX	+	CAPEX
Total UnitCost	C_{ff}	+	$\sum_{s=t_0}^t \varphi_s I_{fs} \alpha(r, T_f)$
$UC_{ff}(w, v) =$	$\frac{\sum_a N_{fa} w_{fa} + \sum_{s=t_0}^t \sum_a \varphi_s n_{fas} v_{fa} \alpha(r, T_g)}{\sum_a N_{fa} w_{fa} + \sum_{s=t_0}^t \sum_a \varphi_s n_{fas} v_{fa} \alpha(r, T_g)}$		
	$\sum_a N_{fa} w_{fa}$	+	$\sum_{s=t_0}^t \sum_a \varphi_s n_{fas} v_{fa} \alpha(r, T_g)$
	OPEX Grid Size		CAPEX Grid Size
	<div style="border-top: 1px solid black; width: 100%; margin-top: 5px;"></div>		<div style="border-top: 1px solid black; width: 100%; margin-top: 5px;"></div>
	OpEx UnitCost		CapEx UnitCost



Three efficiencies

OpEx efficiency is

$$\text{OpEx } E^i = \min \{ \text{OpEx UC}^k \} / \text{OpEx UC}^i$$

CapEx efficiency is

$$\text{CapEx } E^i = \min \{ \text{CapEx UC}^k \} / \text{CapEx UC}^i$$

Total efficiency is

$$\text{Total } E^i = \min \{ \text{Total UC}^k \} / \text{Total UC}^i$$



First problem

Partial measures may be misleading:

- A TSO may have
lower Opex UC
lower CapEx UC – and yet
higher Total UC !
- Known as the Fox Paradox (Fox(2003))

Example

TSO	OpEx UC	CapEx UC	Total UC
A	1/2	1/4	$2/6=0.33$
B	0.15/0.2	2.1/8	$2.25/8.2= 0.27$

Explanation

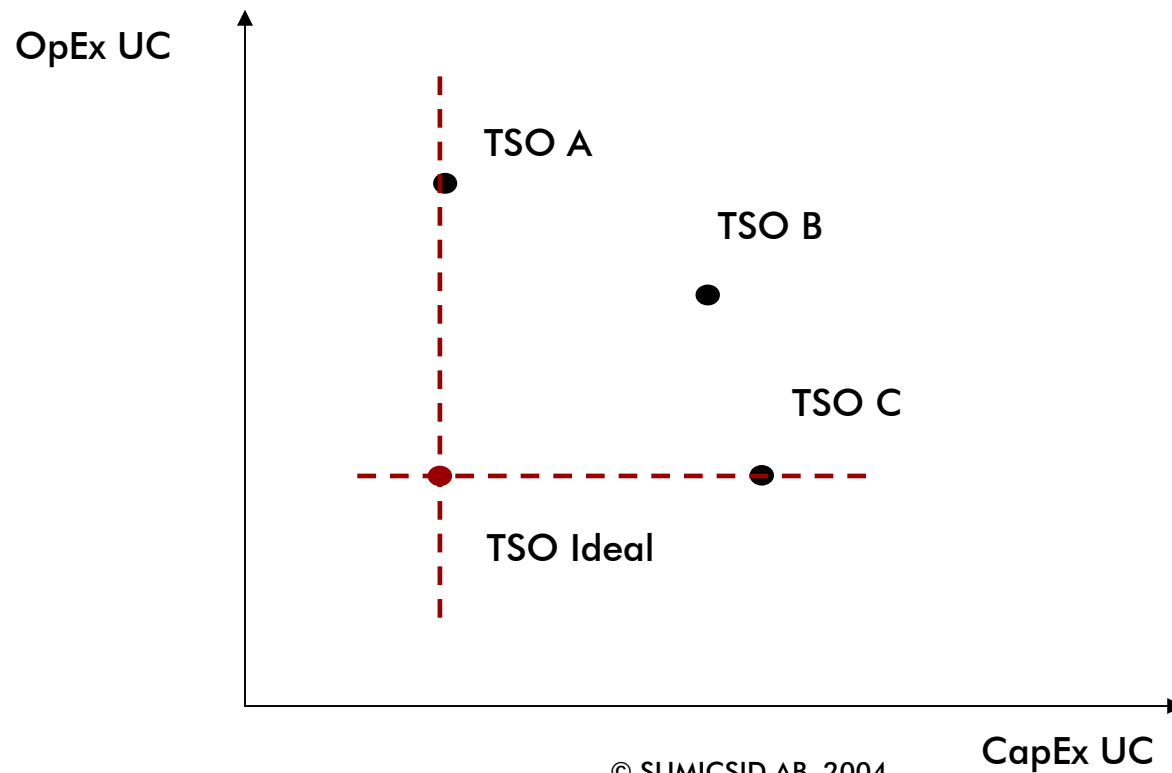
- The relatively more efficient activities (investments) plays a larger part in B



Second problem

Partial measures may be misleading:

- Partial benchmarks make misleading comparisons
- Real units may be compared to non-feasible ideals.





Solutions (1)

Move to absolute values

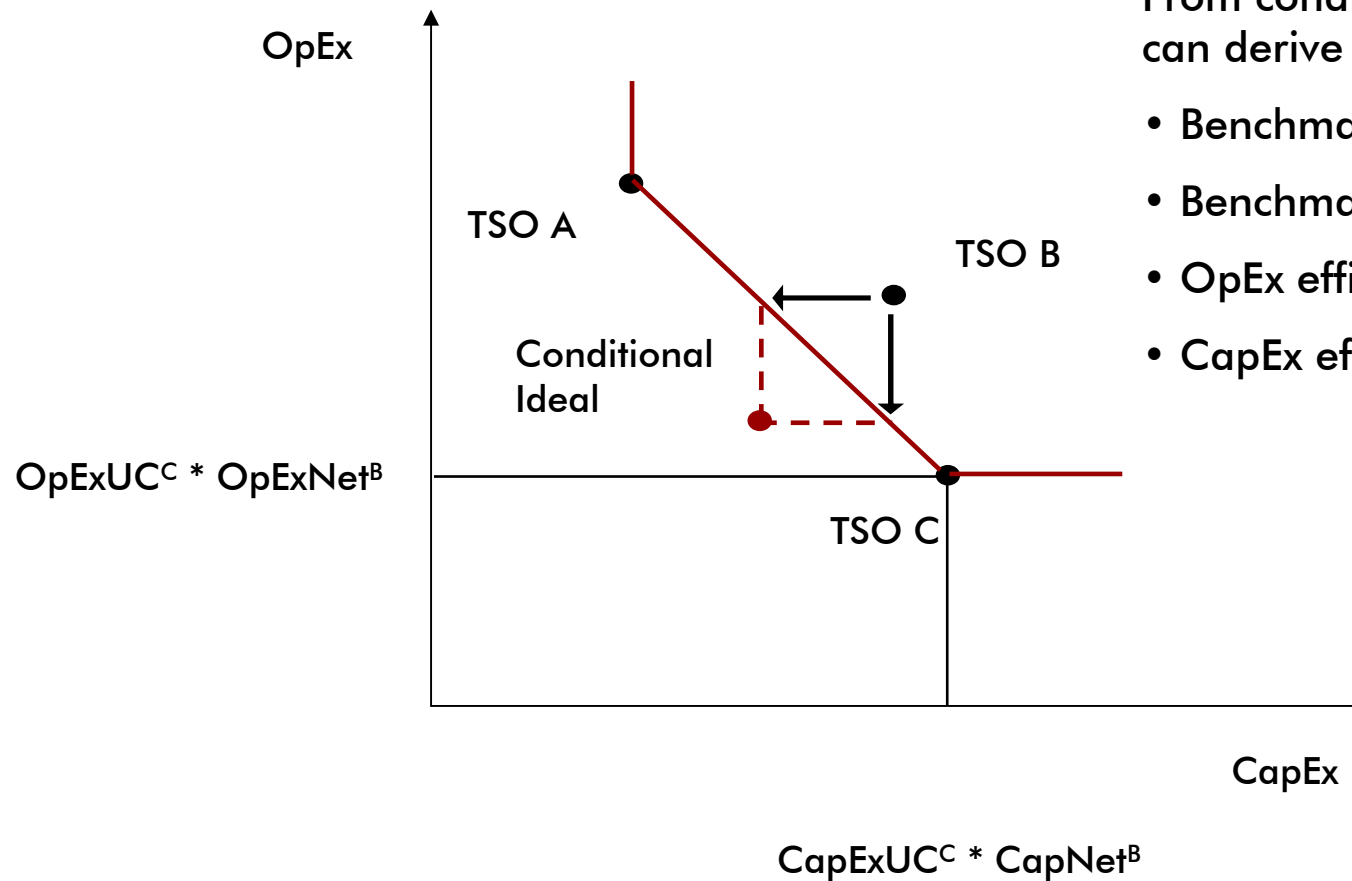
- Similar to input iso-quants
- Solves base / weight problem
- Outfoxing the fox

Move to conditional benchmarks

- Sub-vector approach
- Directional efficiency
- Different scope assumptions



Solutions (2)



From conditional ideal we can derive new conditional

- Benchmark UC in OpEx
- Benchmark UC in CapEx
- OpEx efficiency
- CapEx efficiency



Dynamics



Importance

Absolute levels may not be the most

- Relevant for incentive purposes
- Fair to incumbent management

Dynamic developments may be more important

- Total, OpEx and CapEx Unit Costs
- Total, OpEx and CapEx (Conditional) Efficiency



Performance measure

Let $E^i(s,t)$ be

Efficiency of TSOⁱ's
performance in period s
against technology in period t

$E^i(s,t)$ could be

- Total efficiency
- OpEx efficiency
- CapEx efficiency
- Inverse of UC
- Inverse of OpEx UC
- Inverse of CapEx UC



Malmquist index

TSOⁱ's improvement from period s to period t:

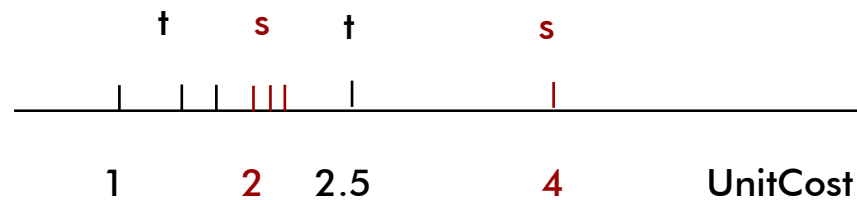
Malmquist index:
$$M^i(s, t) = \sqrt{\frac{E^i(t, s) E^i(t, t)}{E^i(s, s) E^i(s, t)}}$$

Intuition

- We compare efficiency in period t to period s.
- The base technology can be either s or t technology, so we take geometric mean
- Improvements make nominator larger than denominator.
- $M > 1$ corresponds to progress.



Malmquist example



Malmquist index:

$$M^i(s, t) = \sqrt{\frac{E^i(t, s) E^i(t, t)}{E^i(s, s) E^i(s, t)}} = \sqrt{\frac{\frac{2}{2.5} \frac{1}{2.5}}{\frac{2}{4} \frac{1}{4}}} = \frac{4}{2.5}$$

OBS: Special simple case.

Since output is the same and input is one dimensional, the base is not important.

In general, with 1 input 1 output, :

$$M = [\text{out}^t / \text{out}^s] / [\text{in}^t / \text{in}^s] = \text{out growth} / \text{in growth}$$



Malmquist decomposition

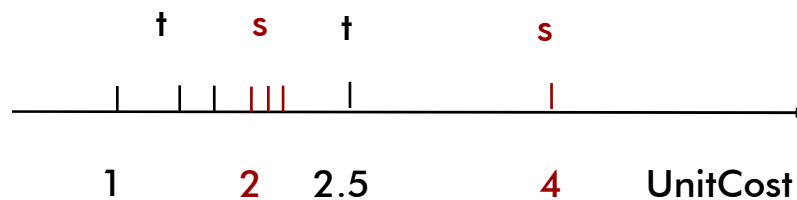
Decomposition:

$$M^i(s, t) = \sqrt{\frac{TE^i(t, s) TE^i(t, t)}{TE^i(s, s) TE^i(s, t)}} = \underbrace{\sqrt{\frac{TE^i(t, s) TE^i(s, s)}{TE^i(t, t) TE^i(s, t)}}}_{TC} \quad \square \quad \underbrace{\frac{TE^i(t, t)}{TE^i(s, s)}}_{EC}$$

Technical change
(Frontier shift)

Efficiency change
(Catch-Up)

Example:



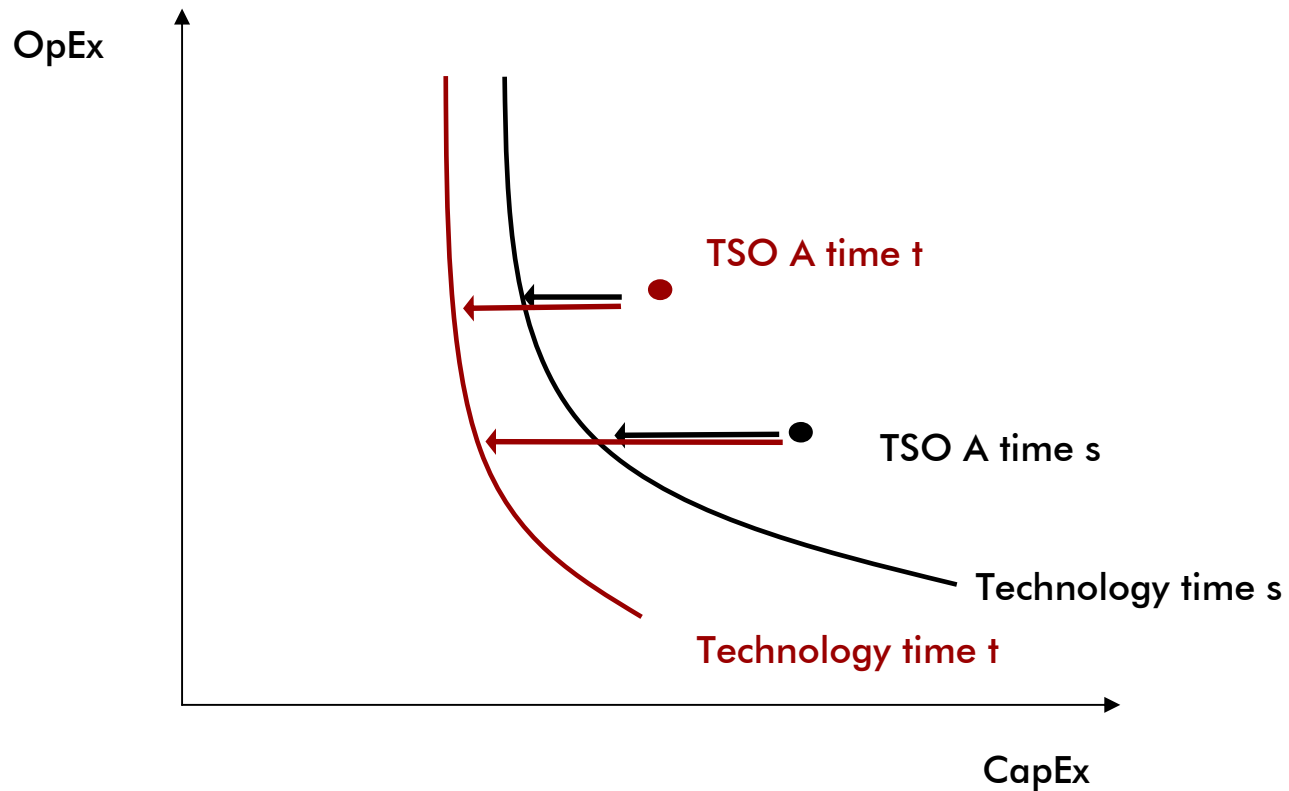
$$\sqrt{\frac{2/2.5 \cdot 2/4}{1/2.5 \cdot 1/4}}$$

$$\square \quad \frac{1/2.5}{2/4} = 2 \quad \square \quad \frac{4}{5}$$



Extensions

We apply the same logic to the conditional measures:





Chaining over several periods

For multi-period decomposition, we would like to have

$$I(1,2) \times I(2,3) = I(1,3)$$

Malquist fails this circular test

- Unless technical change is so-called Hicks-neutral.
- So do most other indices

Remedy

- Fix the base technology
- E.g. last period's technology
- Or pooled technology

Drawback

- The result is base dependent



Malmquist merits

Merits

- No behavioral assumptions required
- No price information (output values) required
- Tells a story
- (May also think of it as a Fisher index with fixed input and output prices)

Potential problems

- Malmquist fails circular test. Remedy: Fixed base.
- Enough data for estimation ?



Conclusions



Summing up

Comparability

- ECOM+ assumptions
- Ways to relax scale and scope assumptions

Decomposition

- The Fox in implicit ECOM+ usage
- Six UC and Efficiencies: Total Cost, OpEx and CapEx
- More relevant (conditional) measures

Dynamics

- Malmquist productivity and its decomposition
- A series of 6+ dynamic measures



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